ILLINOIS INSTITUTE OF TECHNOLOGY Department of Applied Mathematics and IIT SIAM Student Chapter Math Weekly Problem Competition

Friday, October 03, 2014

Two circles of radius 1 are tangent to each other at point Q. PQ and QR are diameters of the two circles. From P a tangent is drawn to the circle with diameter QR, and from R a parallel tangent is drawn to the circle with diameter PQ. Find the distance d between two tangent lines.



Solution. The distance is $\frac{4}{3}$. Let *S* and *T* be the centers of the circles. The perpendicular distance from *T* to the upper tangent line is 1, and its distance from the lower tangent line is the same as that from *S* to the upper tangent line. This distance is $\frac{1}{3}$, by similar triangles, so $d = \frac{4}{3}$.



Good Luck! Have fun and enjoy Mathematics!