**Instructions.** Write all answers clearly on one piece of paper, and put all group members' names on the top of the paper. If you talk, you must do so **very quietly**!

- 1. Explain what property distinguishes a group isomorphism from a group homomorphism.
- 2. What is the definition of the kernel of a group homomorphism?
- 3. (True/False) The kernel of a homomorphism from G to some other group is a subgroup of G.
- 4. (True/False) Let  $\phi : G \to \overline{G}$  be a homomorphism that is *onto*  $\overline{G}$ . Let  $x, y \in \overline{G}$ . It is possible for the preimages of x and y under  $\phi$  to have different sizes. (That is, it is possible for  $|\phi^{-1}(x)| \neq |\phi^{-1}(y)|$ .)
- 5. (True/False) All group isomorphisms are group homomorphisms.