

PRINT Last name: _____ First name: _____

Signature: _____ Student ID: _____

Instructions: Show work for full credit. No notes, calculators, hats, cell phones, or aids of any kind. 15-minute time limit. By signing your name you agree that all work is your own.

Clearly circle or otherwise indicate your answer in order to get credit.

Questions 1-5 are 1pt each with no partial credit.

Questions 6-7 are 2pts each, and all work must be shown.

- Which of the following propositions is correct?
 - The inverse of the implication $p \rightarrow q$ is logically equivalent to $p \rightarrow q$.
 - The converse of the implication $p \rightarrow q$ is logically equivalent to the inverse of $p \rightarrow q$.
 - The contrapositive of the implication $p \rightarrow q$ is logically equivalent to the inverse of $p \rightarrow q$.
 - The converse of the implication $p \rightarrow q$ is logically equivalent to the contrapositive of $p \rightarrow q$.

- If x , y , and z are real numbers, $x < y < z$ means that x is less than y and y is less than z . Which of the following is the negation of $x < y < z$?
 - $x \geq y \geq z$
 - $x \geq y$ or $y \geq z$
 - $x > z$
 - $x > y > z$

- Which of the following is the negation of the statement "I drive to work if and only if it is rainy?"
 - If I drive to work, then it is not rainy.
 - I drive to work if it is not rainy.
 - I drive to work if and only if it is not rainy.
 - I do not drive to work if and only if it is not rainy.
 - I do not drive to work if it is not rainy.

- Suppose r and w are the propositions
 - r : "it is rainy"
 - w : "it is windy"Express in English a compound proposition that is logically equivalent to $w \rightarrow \neg r$.
 - If it is rainy, then it is not windy.
 - It is windy, but not rainy.
 - Whenever it is not windy, it is rainy.
 - Being windy is sufficient for it to be rainy.

5. Suppose m and a represent the propositions:

m : “you are a member of the committee”

a : “you attend the meeting.”

Express in symbols the compound proposition

“To be a member of the committee it is necessary that you attend the meeting.”

(a) $\neg m \rightarrow a$

(b) $a \rightarrow \neg m$

(c) $m \rightarrow a$

(d) $a \rightarrow m$

6. Circle or otherwise indicate the rows of the truth table for which the following compound proposition is *true*:

$$(p \leftrightarrow \neg q) \oplus (q \wedge r)$$

p	q	r	
T	T	T	
T	T	F	
T	F	T	
T	F	F	
F	T	T	
F	T	F	
F	F	T	
F	F	F	

7. Use the truth table to prove the following logical equivalence:

$$(p \rightarrow q) \vee (p \rightarrow r) \equiv p \rightarrow (q \vee r)$$

(This logical equivalence might be helpful in identifying an alternative strategy for a direct proof.)

p	q	r	
T	T	T	
T	T	F	
T	F	T	
T	F	F	
F	T	T	
F	T	F	
F	F	T	
F	F	F	

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Questions 1-5 are 1pt each with no partial credit.

Questions 6-7 are 2pts each, and all work must be shown.

1. Suppose r and w are the propositions

r : "it is rainy"

w : "it is windy"

Express in English a compound proposition that is logically equivalent to $w \rightarrow \neg r$.

- (a) Being windy is sufficient for it to be rainy.
 - (b) If it is rainy, then it is not windy.
 - (c) It is windy, but not rainy.
 - (d) Whenever it is not windy, it is rainy.
2. Which of the following is the negation of the statement "I drive to work if and only if it is rainy?"
- (a) I drive to work if it is not rainy.
 - (b) I do not drive to work if it is not rainy.
 - (c) I do not drive to work if and only if it is not rainy.
 - (d) If I drive to work, then it is not rainy.
 - (e) I drive to work if and only if it is not rainy.
3. If x , y , and z are real numbers, $x < y < z$ means that x is less than y and y is less than z . Which of the following is the negation of $x < y < z$?
- (a) $x > y > z$
 - (b) $x \geq y \geq z$
 - (c) $x > z$
 - (d) $x \geq y$ or $y \geq z$

4. Suppose m and a represent the propositions:

m : "you are a member of the committee"

a : "you attend the meeting."

Express in symbols the compound proposition

"To be a member of the committee it is necessary that you attend the meeting."

- (a) $\neg m \rightarrow a$
- (b) $m \rightarrow a$
- (c) $a \rightarrow \neg m$
- (d) $a \rightarrow m$

5. Which of the following propositions is correct?

- (a) The converse of the implication $p \rightarrow q$ is logically equivalent to the inverse of $p \rightarrow q$.
- (b) The converse of the implication $p \rightarrow q$ is logically equivalent to the contrapositive of $p \rightarrow q$.
- (c) The inverse of the implication $p \rightarrow q$ is logically equivalent to $p \rightarrow q$.
- (d) The contrapositive of the implication $p \rightarrow q$ is logically equivalent to the inverse of $p \rightarrow q$.

6. Circle or otherwise indicate the rows of the truth table for which the following compound proposition is *false*:

$$(p \vee \neg q) \oplus (q \leftrightarrow r)$$

p	q	r	
T	T	T	
T	T	F	
T	F	T	
T	F	F	
F	T	T	
F	T	F	
F	F	T	
F	F	F	

7. Use the truth table to prove the following logical equivalence:

$$(p \rightarrow r) \wedge (q \rightarrow r) \equiv (p \vee q) \rightarrow r$$

(This logical equivalence might be helpful in identifying an alternative strategy for a direct proof.)

p	q	r	
T	T	T	
T	T	F	
T	F	T	
T	F	F	
F	T	T	
F	T	F	
F	F	T	
F	F	F	