



Scalable Preconditioners for Coupled Plasma/Neutral Boundary Transport Simulations

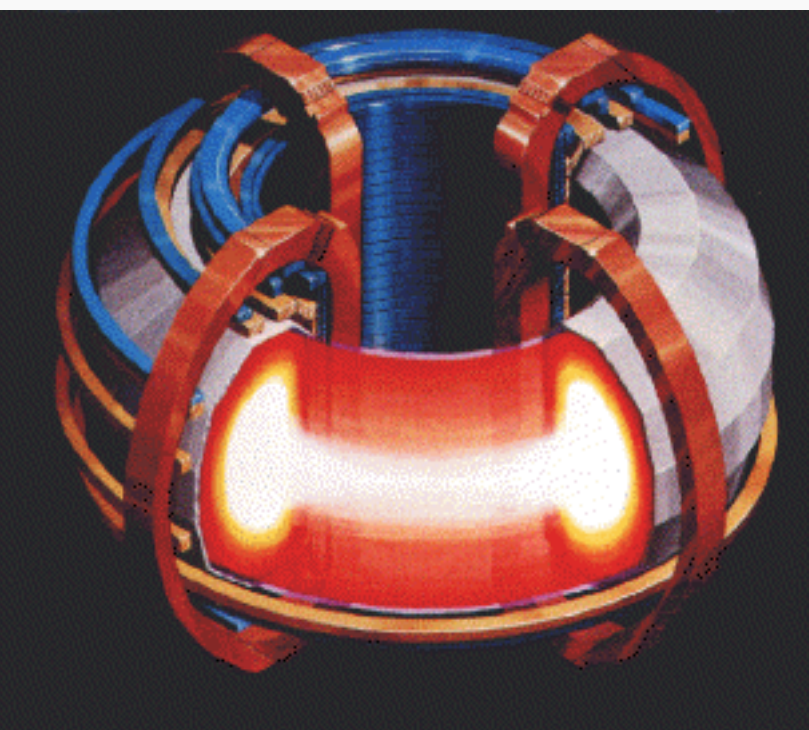
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Introduction

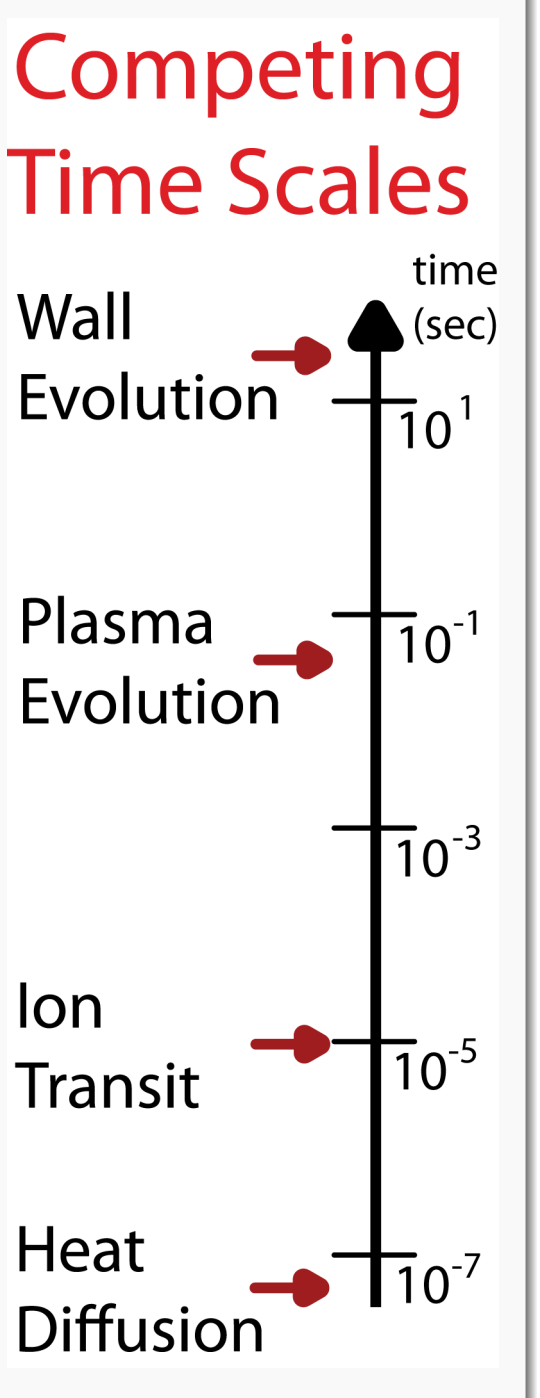
- We study simulations of the edge region of a Tokamak magnetic confinement fusion reactor using UEDGE.
- UEDGE is a 2D parallel edge plasma application developed by T. Rognlien et al. (LLNL)
- UEDGE is one of the edge plasma transport components in FACETS.
- FACETS: Framework Application for Core-Edge Transport Simulations based at Tech-X Corporation
- PI: John Cary, <https://www.facetsproject.org>
- FACETS goal: Strong coupling between core, edge and wall Tokamak regions during simulation



Governing Physics

UEDGE uses a fluid transport model, conserving particles, momentum and energy.

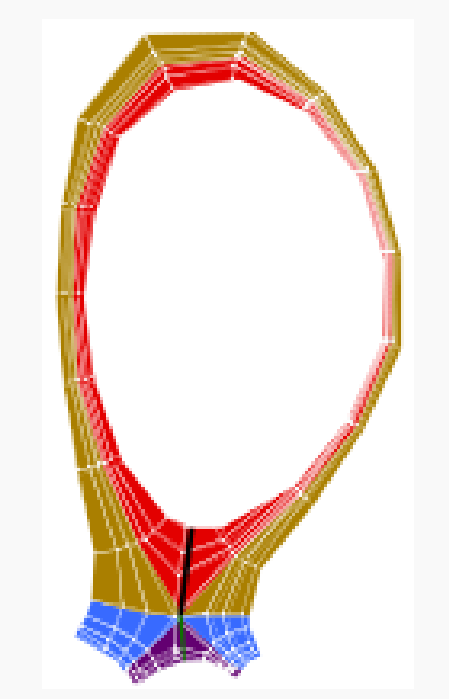
- Simulations use $\Delta t \in [10^{-4}, 10^{-3}]$ sec, appropriate for coupling to time-dependant core models.
- Coupled plasma/neutral simulations involve a large range of spatial and temporal scales.
- Several coupled variables interact in the basic simulation:
 - Deuterium ion D^+ temperature
 - Deuterium ion D^+ density
 - Deuterium ion D^+ parallel velocity
 - Electron e temperature
 - Neutral Deuterium D density
- Strong nonlinearities can yield ill-conditioned simulations
- Impurities in the plasma arise from:
 - Plasma sputtering of material walls, and
 - Edge transport competing with ionization/recombination.
 - Solving each charge state (or bundle) creates large systems.



Motivating a Physics Preconditioner

Physics issues to consider for computational stability/accuracy/efficiency:

- Solving plasma and neutral equations on the same mesh simplifies their strong coupling; this is helpful to ensure an accurate simulation.
- Wall particle recycling and ionization can result in long physical times to reach equilibrium; this competes with the fast edge plasma transport.
- To accommodate the dominant plasma transport, the discretization is highly anisotropic.
- For standard Δt the plasma terms are well-conditioned enough to use an easily scalable preconditioner such as Additive Schwarz.
- However, neutral collisional diffusive transport is isotropic, and very ill-conditioned on an anisotropic mesh.



Radial width is much greater than poloidal

This physical knowledge implies that *separate* methods should be used to precondition the plasma and neutral terms within the nonlinear solver.

Designing a Physics Preconditioner: FieldSplit

1D radial partition
Additive Schwarz Preconditioner

Only coupling within a partition is retained, and all partitions **must** be preconditioned similarly

Important coupling within fields B and C are **ignored** because of their distance in the domain

Additional overlap requires increased message passing

Sample grid

- Field A: All Plasma
- Field B: Neutral density
- Field C: Neutral velocity

Field A generally has many variables and is weakly coupled poloidally.

Fields B and C are coupled throughout the domain.

FieldSplit Preconditioner

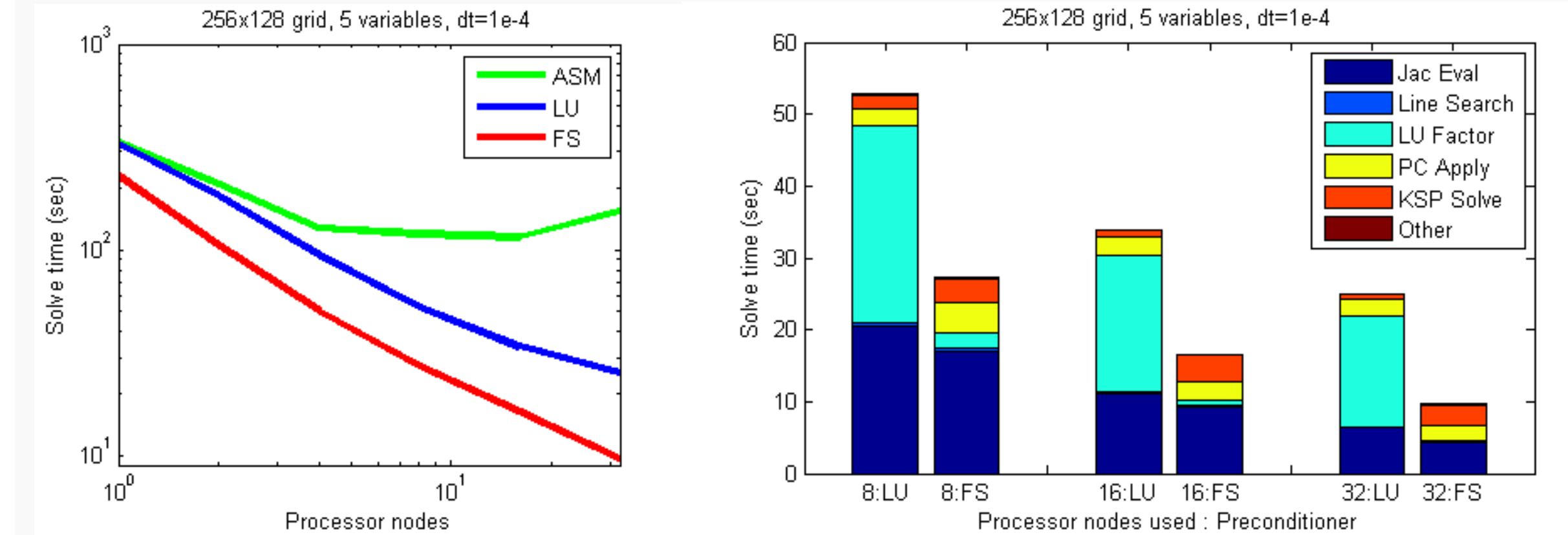
Different preconditioners may be used for each component in FieldSplit:

- Additive Schwarz
- Algebraic Multigrid
- Full LU

Optional retention of coupling between fields via Schur complement

Results: FieldSplit Preconditioning

- Initial FieldSplit structure - 2 separate fields preconditioned individually:
 - Field 1: 4 plasma terms solved with Additive Schwarz
 - Field 2: 1 neutral term solved with Algebraic Multigrid
- Component preconditioners are added together
- Coupling terms between fields are disregarded during preconditioning.

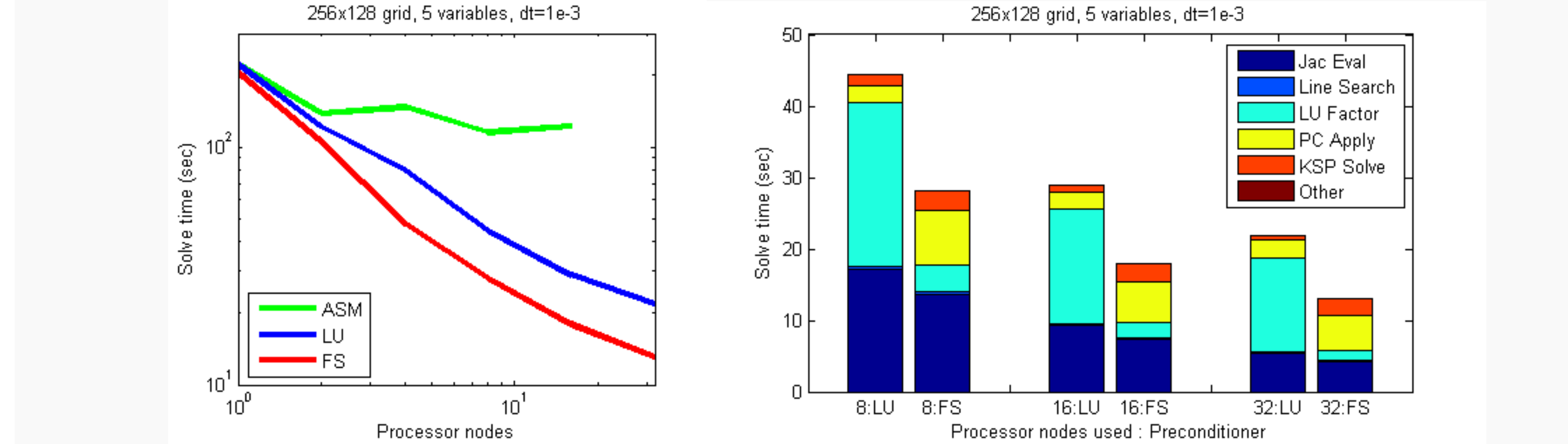


Solver	NP=32 results	KSP its Time (sec)
ASM	1585	154
LU	7	25
FS	44	10

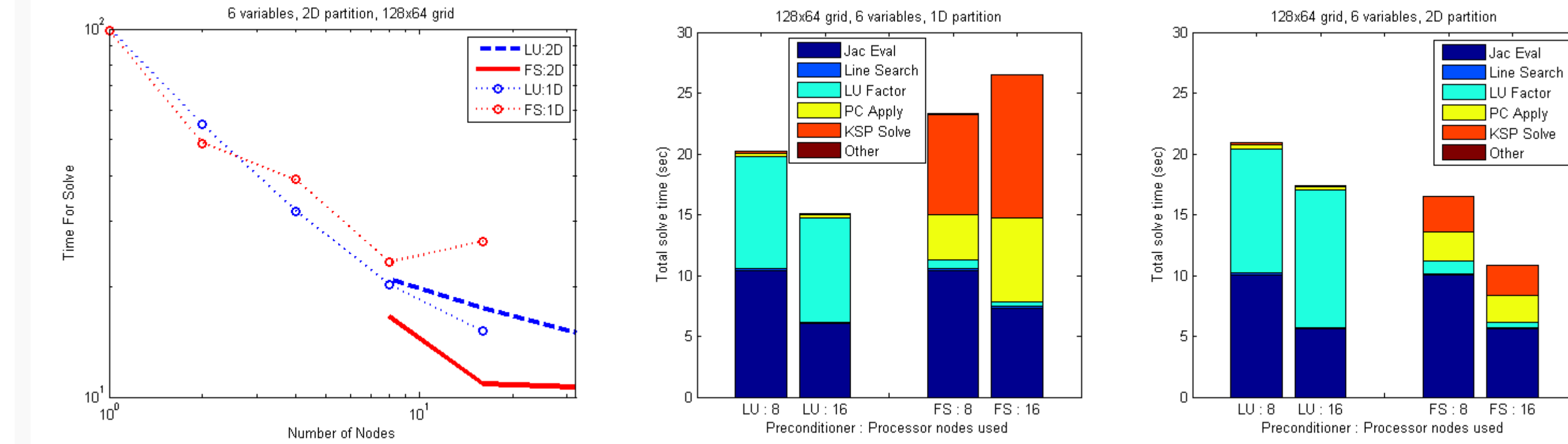
- By handling the troublesome fields (neutral gases) separately we can use a more scalable solver on the easier fields (plasma).
- 1D partitioning allows for the majority of fields (plasma) to be on their more optimal domain.

Results: Scalability for More Complex Problems

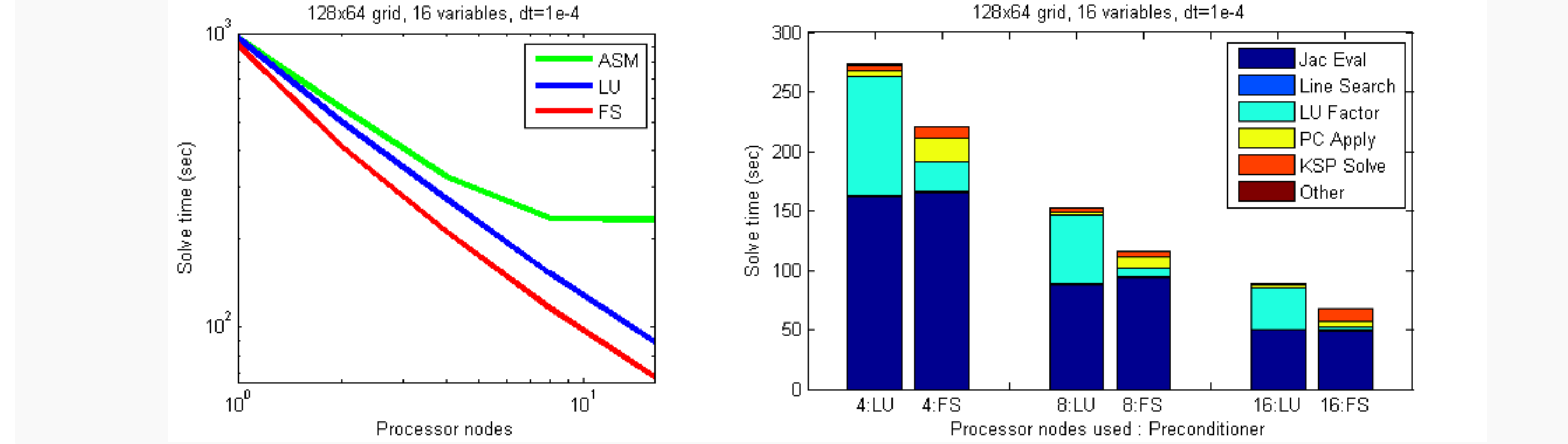
- FieldSplit performs well for larger time steps, so long as the plasma terms can still be solved scalably.



- Initially the neutral D velocity was computed with a simpler algebraic model. Below are results with its inclusion in the nonlinear solve.
- A 2D partitioning is preferred for this problem, which is first available at NP=8.

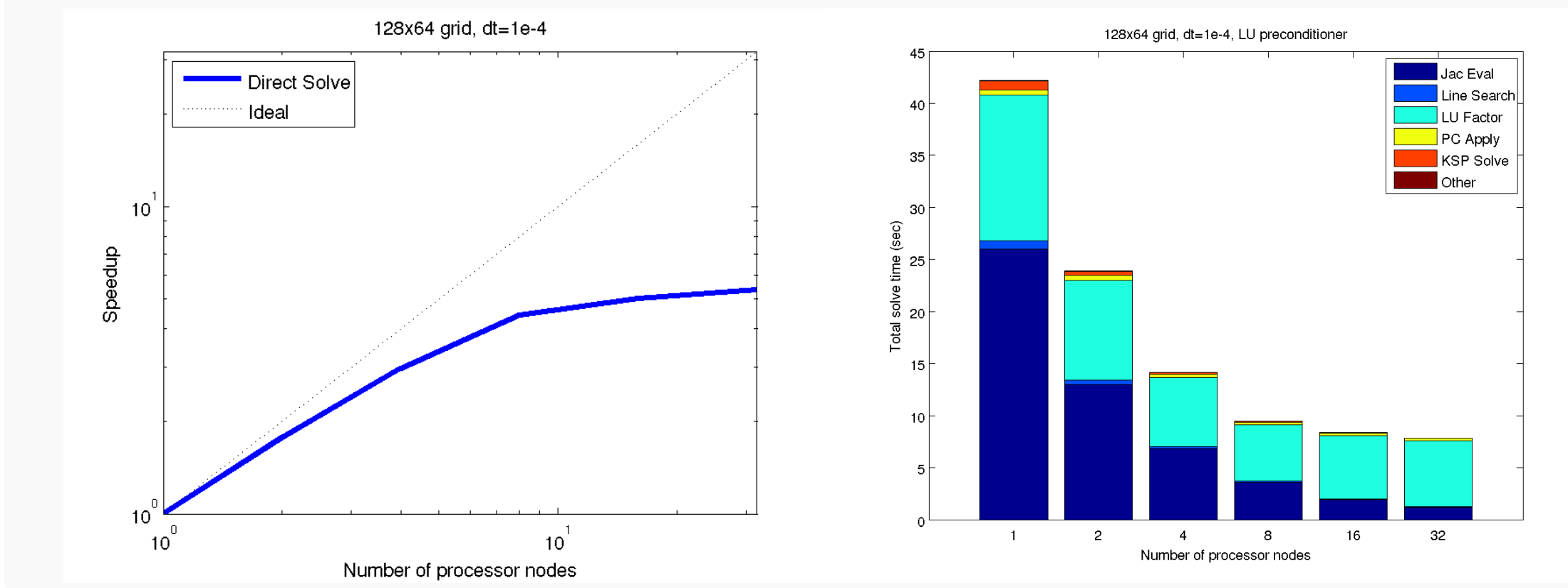


- We also enjoy improved performance in the presence of a Neon impurity and the 11 new individual fields added as a result.



Algorithms

- Implicit time discretization with nonlinear solves via preconditioned Jacobian-free Newton-Krylov
 - The choice of preconditioner is vital to achieving scalability
- PETSc is used to conduct the simulation in parallel
- Early experiments showed limited scalability
 - The direct solver becomes overwhelmed by the cost of LU factorization and associated communication.



Conclusions

- FieldSplit overcomes a major obstacle to parallel scalability for an implicit coupled neutral/plasma edge model.
 - This allows greatly reduced runtimes when using multiple processors.
 - Little code manipulation is required.
- Jacobian-free Newton-Krylov within PETSc using FieldSplit preconditioning provides flexibility for optimizations such as
 - Redundant preconditioning on comparatively small fields,
 - Variable Additive Schwarz overlap, and
 - Jacobian lagging both within and across time steps.

Future Work

- As different species (e.g., He and C) are added and larger Δt used, how can FieldSplit be optimized?
- The goal of the FACETS project is Core-Edge-Wall coupling
 - How can this physics preconditioning be applied in a multiphysics setting?
 - What techniques developed here can be used in 3D edge codes, e.g., BOUT++?
- Coupling terms can be retained via the Schur complement.
 - Cost is greater than Additive FieldSplit.
 - While not needed so far, will this coupling be useful in multiphysics preconditioning?

Acknowledgements

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