

# SLEPc: Scalable Library for Eigenvalue Problem Computations

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### Outline



Overview of SLEPc



#### Basic Usage

- Eigenvalue Solvers
- Spectral Transformation
- SVD Solvers







### Introduction



#### **Eigenvalue Problems**

#### Consider the following eigenvalue problems

Standard EigenproblemGeneralized Eigenproblem
$$Ax = \lambda x$$
 $Ax = \lambda Bx$ 

where

- >  $\lambda$  is a (complex) scalar: *eigenvalue*
- x is a (complex) vector: eigenvector
- Matrices A and B can be real or complex
- ▶ Matrices A and B can be symmetric (Hermitian) or not
- ▶ Typically, *B* is symmetric positive (semi-) definite



#### Solution of the Eigenvalue Problem

There are n eigenvalues (counted with their multiplicities)

Partial eigensolution: nev solutions  $\lambda_0, \lambda_1, \dots, \lambda_{nev-1} \in \mathbb{C}$  $x_0, x_1, \dots, x_{nev-1} \in \mathbb{C}^n$  nev = number of eigenvalues / eigenvectors (eigenpairs)



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Different requirements:

- Compute a few of the dominant eigenvalues (largest magnitude)
- Compute a few  $\lambda_i$ 's with smallest or largest real parts
- Compute all  $\lambda_i$ 's in a certain region of the complex plane



#### Spectral Transformation

A general technique that can be used in many methods

$$Ax = \lambda x \qquad \Longrightarrow \qquad Tx = \theta x$$



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- Convergence is usually improved (better separation)



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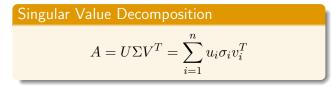
Shift of Origin  
$$T_S = A + \sigma I$$
Shift-and-invert  
 $T_{SI} = (A - \sigma I)^{-1}$ Cayley  
 $T_C = (A - \sigma I)^{-1}(A + \tau I)$ 

Drawback: T not computed explicitly, linear solves instead



#### Singular Value Problems

# Consider the SVD decomposition of a rectangular matrix $A \in \mathbb{R}^{m \times n}$



where

- $\triangleright \sigma_1, \sigma_2, \ldots, \sigma_n$ : singular values
- ▶  $u_1, u_2, \ldots, u_n$ : left singular vectors
- $\triangleright$   $v_1, v_2, \ldots, v_n$ : right singular vectors



#### Solution of the Singular Value Problem

There are n singular values (counted with their multiplicities)

Partial solution: nsv solutions

 $\sigma_0, \sigma_1, \dots, \sigma_{nsv-1} \in \mathbb{R}$  $u_0, u_1, \dots, u_{nsv-1} \in \mathbb{R}^m$  $v_0, v_1, \dots, v_{nsv-1} \in \mathbb{R}^n$ 

nsv = number of singular values / vectors (singular triplets)

• Compute a few smallest or largest  $\sigma_i$ 's



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Alternatives:

• Solve eigenproblem  $A^T A$ 

► Solve eigenproblem 
$$H(A) = \begin{bmatrix} 0^{m \times m} & A \\ A^T & 0^{n \times n} \end{bmatrix}$$

Bidiagonalization





# **Overview of SLEPc**



- Various problem characteristics: Problems can be real/complex, Hermitian/non-Hermitian
- Many ways of specifying which solutions must be sought
- ► Many formulations: not all eigenproblems are formulated as simply  $Ax = \lambda x$  or  $Ax = \lambda Bx$



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- Many ways of specifying which solutions must be sought
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Goal: provide a uniform, coherent way of addressing these problems

- Internally, solvers can be quite complex (deflation, restart, ...)
- Spectral transformations can be used irrespective of the solver
- Repeated linear solves may be required
- SVD can be solved via associated eigenproblem or bidiagonalization



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- Spectral transformations can be used irrespective of the solver
- Repeated linear solves may be required
- SVD can be solved via associated eigenproblem or bidiagonalization

Goal: hide eigensolver complexity and separate spectral transform



#### What Users Need

- Abstraction of mathematical objects: vectors and matrices
- Efficient linear solvers (direct or iterative)
- Easy programming interface
- Run-time flexibility, full control over the solution process
- Parallel computing, mostly transparent to the user

- State-of-the-art eigensolvers
- Spectral transformations
- SVD solvers



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# What Users Need

#### Provided by PETSc

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- Easy programming interface
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#### Provided by SLEPc

- State-of-the-art eigensolvers
- Spectral transformations
- SVD solvers



#### Summary

**PETSc**: Portable, Extensible Toolkit for Scientific Computation

Software for the scalable (parallel) solution of algebraic systems arising from partial differential equation (PDE) simulations

- Developed at Argonne National Lab since 1991
- ▶ Usable from C, C++, Fortran77/90
- Focus on abstraction, portability, interoperability
- Extensive documentation and examples
- Freely available and supported through email

http://www.mcs.anl.gov/petsc

Current version: 3.0.0 (released Dec 2008)



#### Summary

SLEPc: Scalable Library for Eigenvalue Problem Computations

A *general* library for solving large-scale sparse eigenproblems on parallel computers

- For standard and generalized eigenproblems
- For real and complex arithmetic
- For Hermitian or non-Hermitian problems

Also support for the partial SVD decomposition

http://www.grycap.upv.es/slepc

Current version: 3.0.0 (released Feb 2009)



# Structure of SLEPc (1)

SLEPc extends PETSc with three new objects: EPS, ST, SVD

#### EPS: Eigenvalue Problem Solver

- The user specifies an eigenproblem via this object
- Provides a collection of eigensolvers
- Allows the user to specify a number of parameters (e.g. which portion of the spectrum)



# Structure of SLEPc (2)

#### ST: Spectral Transformation

- ▶ Used to transform the original problem into  $Tx = \theta x$
- Always associated to an EPS object, not used directly



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#### ST: Spectral Transformation

- ▶ Used to transform the original problem into  $Tx = \theta x$
- Always associated to an EPS object, not used directly

#### SVD: Singular Value Decomposition

- The user specifies the SVD problem via this object
- Transparently provides the associated eigenproblems or a specialized solver



### PETSc/SLEPc Numerical Components

PETSc

Nonli	near Syst	ems	Time Steppers			
Line Search	Trust Region	Other	Euler	Backward Euler	Pseudo Time Step	Other

Krylov Subspace Methods								
GMRES	CG	CGS	Bi-CGStab	TFQMR	Richardson	Chebychev	Other	

Preconditioners								
Additive Schwarz	Block Jacobi	Jacobi	ILU	ICC	LU	Other		

Matrices							
Compressed Sparse Row	Block Compressed Sparse Row	Block Diagonal	Dense	Other			

	Index Sets						
Vectors	Indices	Block Indices	Stride	Other			



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	Krylov Subspace Methods								
G	MRES	CG	CGS	Bi-CGStab	TFQMR	Richardson	Chebychev	Other	

SVD Solvers								
Cross Product	Cyclic Matrix	Lanczos	Thick Res. Lanczos					

Eigensolvers								
Krylov-Schur	Arnoldi	Lanczos	Other					

Preconditioners								
Additive Schwarz	Block Jacobi	Jacobi	ILU	ICC	LU	Other		

Matrices								
Compressed Sparse Row	Block Compressed Sparse Row	Block Diagonal	Dense	Other				

	Index Sets				
Vectors	Indices	Block Indices	Stride	Other	

Spectral Transform					
Shift	Shift-and-invert	Cayley	Fold		





### **Basic Usage**



### EPS: Basic Usage

Usual steps for solving an eigenvalue problem with SLEPc:

- 1. Create an EPS object
- 2. Define the eigenvalue problem
- 3. (Optionally) Specify options for the solution
- 4. Run the eigensolver
- 5. Retrieve the computed solution
- 6. Destroy the EPS object

All these operations are done via a generic interface, common to all the eigensolvers





EPS	eps;
Mat	А, В;
Vec	xr, xi;
PetscScalar	kr, ki;

/*	eigensolver context	*/
/*	matrices of Ax=kBx	*/
/*	eigenvector, x	*/
/*	eigenvalue, k	*/





EPS	eps;	/*	eigensolver context	*/
Mat	А, В;	/*	matrices of Ax=kBx	*/
Vec	xr, xi;	/*	eigenvector, x	*/
PetscScalar	kr, ki;	/*	eigenvalue, k	*/

```
EPSCreate(PETSC_COMM_WORLD, &eps);
EPSSetOperators(eps, A, B);
EPSSetProblemType(eps, EPS_GNHEP);
EPSSetFromOptions(eps);
```





EPS	eps;	/*	eigensolver context	*/
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```
EPSSolve(eps);
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EPSSetOperators(eps, A, B);
EPSSetProblemType(eps, EPS_GNHEP);
EPSSetFromOptions(eps);
```

```
EPSSolve(eps);
```

```
EPSGetConverged(eps, &nconv);
for (i=0; i<nconv; i++) {
  EPSGetEigenpair(eps, i, &kr, &ki, xr, xi);
}
```





EPS	eps;	/*	eigensolver context	*/
Mat	А, В;	/*	matrices of Ax=kBx	*/
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}
```

```
EPSDestroy(eps);
```



### Details: Solving the Problem

#### EPSSolve(EPS eps)

Launches the eigensolver

Currently available eigensolvers:

- Power Iteration and RQI
- Subspace Iteration with Rayleigh-Ritz projection and locking
- Arnoldi method with explicit restart and deflation
- Lanczos method with explicit restart and deflation
  - ▶ Reorthogonalization: Local, Partial, Periodic, Selective, Full
- Krylov-Schur (default)

Also interfaces to external software: ARPACK, PRIMME, ...



### Details: Problem Definition

EPSSetOperators(EPS eps, Mat A, Mat B)

Used for passing the matrices that constitute the problem

- A generalized problem  $Ax = \lambda Bx$  is specified by A and B
- For a standard problem  $Ax = \lambda x$  set B=PETSC\_NULL



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- A generalized problem  $Ax = \lambda Bx$  is specified by A and B
- ▶ For a standard problem  $Ax = \lambda x$  set B=PETSC\_NULL

#### EPSSetProblemType(EPS eps, EPSProblemType type)

Used to indicate the problem type

Problem Type	EPSProblemType	Command line key
Hermitian	EPS_HEP	-eps_hermitian
Generalized Hermitian	EPS_GHEP	-eps_gen_hermitian
Non-Hermitian	EPS_NHEP	-eps_non_hermitian
Generalized Non-Herm.	EPS_GNHEP	-eps_gen_non_hermitian



### Details: Specification of Options

EPSSetFromOptions(EPS eps)

Looks in the command line for options related to EPS

For example, the following command line

% program -eps\_hermitian

is equivalent to a call EPSSetProblemType(eps, EPS\_HEP)



### Details: Specification of Options

EPSSetFromOptions(EPS eps)

Looks in the command line for options related to EPS

For example, the following command line

- % program -eps\_hermitian
- is equivalent to a call EPSSetProblemType(eps, EPS\_HEP)

Other options have an associated function call

% program -eps\_nev 6 -eps\_tol 1e-8



### Details: Specification of Options

EPSSetFromOptions(EPS eps)

Looks in the command line for options related to EPS

For example, the following command line

- % program -eps\_hermitian
- is equivalent to a call EPSSetProblemType(eps, EPS\_HEP)

Other options have an associated function call

% program -eps\_nev 6 -eps\_tol 1e-8

#### EPSView(EPS eps, PetscViewer viewer)

Prints information about the object (equivalent to -eps\_view)



## Details: Viewing Current Options

#### Sample output of -eps\_view

```
EPS Object:
  problem type: symmetric eigenvalue problem
 method: krylovschur
  selected portion of spectrum: largest eigenvalues in magnitude
  number of eigenvalues (nev): 1
  number of column vectors (ncv): 16
  maximum dimension of projected problem (mpd): 16
  maximum number of iterations: 100
  tolerance: 1e-07
  dimension of user-provided deflation space: 0
  IP Object:
    orthogonalization method: classical Gram-Schmidt
    orthogonalization refinement: if needed (eta: 0.707100)
  ST Object:
    type: shift
    shift: 0
```



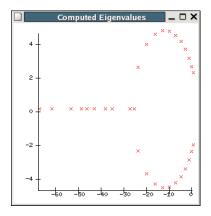


#### EPS: Run-Time Examples

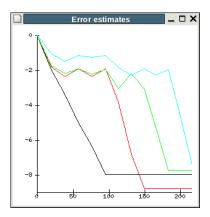
- % program -eps\_view -eps\_monitor
- % program -eps\_type krylovschur -eps\_nev 6 -eps\_ncv 24
- % program -eps\_type arnoldi -eps\_tol 1e-8 -eps\_max\_it 2000
- % program -eps\_type subspace -eps\_hermitian -log\_summary
- % program -eps\_type lapack
- % program -eps\_type arpack -eps\_plot\_eigs -draw\_pause -1
- % program -eps\_type primme -eps\_smallest\_real

### Built-in Support Tools

- Plotting computed eigenvalues
   % program -eps\_plot\_eigs
- Printing profiling information
   % program -log\_summary
- Debugging
   % program -start\_in\_debugger
   % program -malloc\_dump



# Built-in Support Tools



 Monitoring convergence (textually)
 % program -eps\_monitor

SI EPc

 Monitoring convergence (graphically)
 % program -draw\_pause 1 -eps\_monitor\_draw



#### Spectral Transformation in SLEPc

An ST object is always associated to any EPS object

$$Ax = \lambda x \qquad \Longrightarrow \qquad Tx = \theta x$$





## Spectral Transformation in SLEPc

An ST object is always associated to any EPS object

$$Ax = \lambda x \qquad \Longrightarrow \qquad Tx = \theta x$$

- The user need not manage the ST object directly
- $\blacktriangleright$  Internally, the eigensolver works with the operator T
- At the end, eigenvalues are transformed back automatically





## Spectral Transformation in SLEPc

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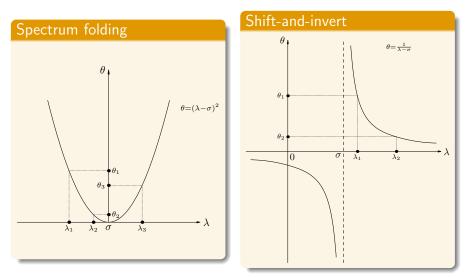
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- The user need not manage the ST object directly
- $\blacktriangleright$  Internally, the eigensolver works with the operator T
- > At the end, eigenvalues are transformed back automatically

ST	Standard problem	Generalized problem
shift	$A + \sigma I$	$B^{-1}A + \sigma I$
fold	$(A + \sigma I)^2$	$(B^{-1}A + \sigma I)^2$
sinvert	$(A - \sigma I)^{-1}$	$(A - \sigma B)^{-1}B$
cayley	$(A - \sigma I)^{-1}(A + \tau I)$	$(A - \sigma B)^{-1}(A + \tau B)$



#### Illustration of Spectral Transformation







#### Accessing the ST Object

The user does not create the ST object

EPSGetST(EPS eps, ST \*st)

Gets the ST object associated to an EPS

Necessary for setting options in the source code



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The user does not create the ST object

EPSGetST(EPS eps, ST \*st)

Gets the ST object associated to an EPS

Necessary for setting options in the source code

Linear Solves. Most operators contain an inverse

Linear solves are handled internally via a KSP object

STGetKSP(ST st, KSP \*ksp)

Gets the KSP object associated to an ST

All KSP options are available, by prepending the  $-st_-$  prefix





#### ST: Run-Time Examples

- % program -eps\_type power -st\_type shift -st\_shift 1.5
- % program -eps\_type power -st\_type sinvert -st\_shift 1.5
- % program -eps\_type power -st\_type sinvert -eps\_power\_shift\_type rayleigh
- % program -eps\_type arpack -eps\_tol 1e-6 -st\_type sinvert -st\_shift 1 -st\_ksp\_type cgs -st\_ksp\_rtol 1e-8 -st\_pc\_type sor -st\_pc\_sor\_omega 1.3



## SVD: Basic Usage

Usual steps for solving an SVD problem with SLEPc:

- 1. Create an SVD object
- 2. Define the problem
- 3. (Optionally) Specify options for the solution
- 4. Run the solver
- 5. Retrieve the computed solution
- 6. Destroy the SVD object

All these operations are done via a generic interface, common to all the SVD solvers





SVD	svd;
Mat	Α;
Vec	u,v;
PetscReal	s;

/*	SVD solver context	*/
/*	matrix for A=USV^T	*/
/*	singular vectors	*/
/*	singular value	*/





svd;	/*	SVD solver context	*/
Α;	/*	matrix for A=USV^T	*/
u,v;	/*	singular vectors	*/
s;	/*	singular value	*/
	A; u,v;	A; /* u,v; /*	A; /* matrix for A=USV^T u,v; /* singular vectors

SVDCreate(PETSC\_COMM\_WORLD, &svd); SVDSetOperator(svd, A); SVDSetFromOptions(svd);





svd;	/*	SVD solver context	*/
Α;	/*	matrix for A=USV^T	*/
u,v;	/*	singular vectors	*/
s;	/*	singular value	*/
	A; u,v;	A; /* u,v; /*	A; /* matrix for A=USV^T u,v; /* singular vectors

SVDCreate(PETSC\_COMM\_WORLD, &svd); SVDSetOperator(svd, A); SVDSetFromOptions(svd);

```
SVDSolve(svd);
```





SVD	svd;	/*	SVD solver context	*/
Mat	A;	/*	matrix for A=USV^T	*/
Vec	u,v;	/*	singular vectors	*/
PetscReal	s;	/*	singular value	*/

```
SVDCreate(PETSC_COMM_WORLD, &svd);
SVDSetOperator(svd, A);
SVDSetFromOptions(svd);
```

```
SVDSolve(svd);
```

```
SVDGetConverged(svd, &nconv);
for (i=0; i<nconv; i++) {
   SVDGetSingularTriplet(svd, i, &s, u, v);
}</pre>
```





SVD	svd;	/*	SVD solver context	*/
Mat	A;	/*	matrix for A=USV^T	*/
Vec	u,v;	/*	singular vectors	*/
PetscReal	s;	/*	singular value	*/

```
SVDCreate(PETSC_COMM_WORLD, &svd);
SVDSetOperator(svd, A);
SVDSetFromOptions(svd);
```

```
SVDSolve(svd);
```

```
SVDGetConverged(svd, &nconv);
for (i=0; i<nconv; i++) {
   SVDGetSingularTriplet(svd, i, &s, u, v);
}</pre>
```

```
SVDDestroy(svd);
```



#### Details: Solving the Problem

#### SVDSolve(SVD svd)

Launches the SVD solver

Currently available SVD solvers:

- Cross-product matrix with any EPS eigensolver
- Cyclic matrix with any EPS eigensolver
- Golub-Kahan-Lanczos bidiagonalization with explicit restart and deflation
- Golub-Kahan-Lanczos bidiagonalization with thick restart and deflation



### Details: Problem Definition and Specification of Options

SVDSetOperators(SVD svd, Mat A)

Used for passing the matrix that constitutes the problem



## Details: Problem Definition and Specification of Options

SVDSetOperators(SVD svd, Mat A)

Used for passing the matrix that constitutes the problem

#### SVDSetFromOptions(SVD svd)

Looks in the command line for options related to SVD

For example, the following command line

% program -svd\_tol 1e-8 -svd\_max\_it 100

is equivalent to a call SVDSetTolerances(eps,1e-8,100)



## Details: Problem Definition and Specification of Options

SVDSetOperators(SVD svd, Mat A)

Used for passing the matrix that constitutes the problem

#### SVDSetFromOptions(SVD svd)

Looks in the command line for options related to SVD

For example, the following command line

% program -svd\_tol 1e-8 -svd\_max\_it 100

is equivalent to a call SVDSetTolerances(eps,1e-8,100)

#### SVDView(SVD svd, PetscViewer viewer)

Prints information about the object (equivalent to -svd\_view)



#### Details: Viewing Current Options

#### Sample output of -svd\_view

```
SVD Object:
 method: trlanczos
  transpose mode: explicit
  selected portion of the spectrum: largest
  number of singular values (nsv): 1
  number of column vectors (ncv): 10
  maximum dimension of projected problem (mpd): 10
  maximum number of iterations: 100
  tolerance: 1e-07
  Lanczos reorthogonalization: two-side
  IP Object:
    orthogonalization method: classical Gram-Schmidt
    orthogonalization refinement: if needed (eta: 0.707100)
```





#### SVD: Run-Time Examples

- % program -svd\_view -svd\_monitor
- % program -svd\_type lanczos -svd\_nsv 6 -svd\_ncv 24
- % program -svd\_type trlanczos -svd\_tol 1e-8 -svd\_max\_it 2000
- % program -svd\_type cross -svd\_eps\_type krylovschur
- % program -svd\_type lapack
- % program -svd\_type lanczos -svd\_monitor\_draw
- % program -svd\_type trlanczos -svd\_smallest





## **Advanced Features**





#### **Options for Subspace Generation**

#### Initial Subspace

- Provide an initial trial subspace, e.g. from a previous computation
- Current support only for a single vector (EPSSetInitialVector)

#### Deflation Subspace

- Provide a deflation space with EPSAttachDeflationSpace
- The eigensolver operates in the restriction to the orthogonal complement
- Useful for constrained eigenproblems or problems with a known nullspace



## Subspace Extraction

In some cases, convergence of the eigensolver may be very slow

 $\rightarrow$  Enhanced subspace extraction: try to extract better approximations from the available subspace

#### Harmonic extraction

- Compute harmonic Ritz values instead of Ritz values
- Useful for computing interior eigenvalues (alternative to the spectral transformation)
- Currently implemented in Krylov-Schur solver
- Other: refined extraction

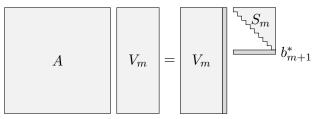




## Computation of Many Eigenpairs

By default, a subspace of dimension  $2\cdot nev$  is used... For large nev, this is not appropriate

Excessive storage and inefficient computation



Strategy: compute eigenvalues in chunks - restrict the dimension of the projected problem

% program -eps\_nev 2000 -eps\_mpd 300



# SLEPc Highlights

- Growing number of eigensolvers
- Seamlessly integrated spectral transformation
- Support for SVD
- Easy programming with PETSc's object-oriented style
- Data-structure neutral implementation
- Run-time flexibility, giving full control over the solution process
- Portability to a wide range of parallel platforms
- ▶ Usable from code written in C, C++ and Fortran
- Extensive documentation



### **Future Directions**

#### Under Development

- Generalized Davidson and Jacobi-Davidson solvers
- Enable computational intervals for symmetric problems

#### Mid Term

- Conjugate Gradient-type eigensolvers
- Non-symmetric Lanczos eigensolver
- Support for other types of eigenproblems: quadratic, structured, non-linear



### More Information



Homepage:

http://www.grycap.upv.es/slepc

Hands-on Exercises:

http://www.grycap.upv.es/slepc/handson

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