## Math 425 - Homework 4

Due Monday 03/11

Unless otherwise instructed, conduct all hypothesis tests at the  $\alpha = .05$  level. The numbers associated with each problem come from various editions of the text, so don't be surprised if they do not match yours.

- 1. Problem 9.14: A librarian claims that, on average, her library's books are more than 20 years old. To test this, a students takes a sample of n = 30 books and notices that they have an average age of  $\bar{X} = 23.8$  and a sample variance of  $s^2 = 67.5$ . Use this sample to conduct a one-tailed test with  $\alpha = .01$  to determine whether the average age to the library books is significantly greater than 20 years ( $\mu > 20$ ).
- 2. *Problem 10.4:* Describe the homogeneity of variance assumption and explain why it is important for the independent-measures (2 sample) t-test.
- 3. Problem 10.5: One sample has  $SS_1 = 48$  and a second has  $SS_2 = 32$ . a) If n = 5 for both samples find each of the sample variances and compute the pooled variance. b) Suppose  $n_1 = 5$  and  $n_2 = 9$ . Again compute the sample and pooled variances. c) Explain the effect that occurred when n was changed.
- 4. Problem 10.9 Two samples received different treatments. The first sample has  $n_1 = 9$  with  $SS_1 = 710$  and the second sample has  $n_2 = 6$  with  $SS_2 = 460$ . a) Compute the pooled variance for the two samples. b) Calculate the estimated standard error for the sample mean difference. c) If the sample mean difference is 10 points, is this enough to reject the null hypothesis using a two-tailed test with  $\alpha = .05$ ? d) If the sample mean difference is 13 points, is this enough to reject  $H_0$  using a two-tailed test with  $\alpha = .05$ ?
- 5. Problem 10.17 I have invented a new style of dancing, that men seem to love and women seem to hate. Conduct a two-tailed test at  $\alpha = .01$  significance on the following data of how much (on a scale of 1 to 100) people love my new dance.

Men	Women
n = 15	n = 15
$\bar{X} = 40.8$	$\bar{X} = 34.0$
SS = 510	SS = 414